

Transformation validation for SSA programs

An approach using value graphs à la Paul Govereau

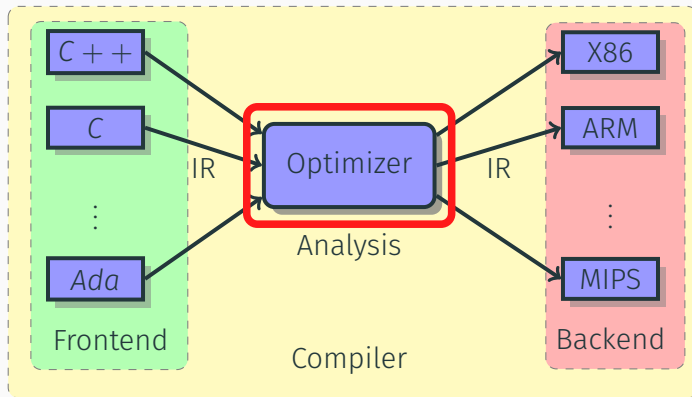
Thomas Rubiano

SAV2019

Motivations

Optimizing compilers

Architecture

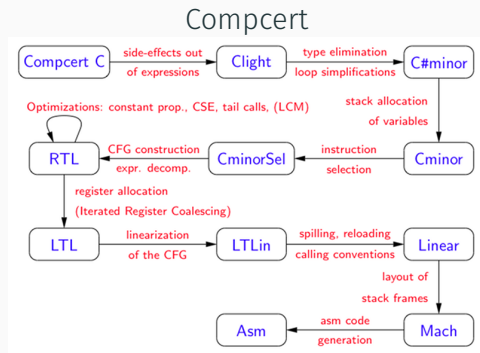


\$ clang -O3

Pass Arguments: -tti -targetlibinfo -tbaa -scoped-noalias -assumption-cache-tracker -profile-summary-info -forceattrs -inferattrs -callsite-splitting -ipsccp -called-value-propagation -globalopt -domtree -mem2reg -deadargelim -domtree -basicaa -aa -loops -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -simplifycfg -basiccg -globals-aa -prune-eh -inline -functionattrs -argpromotion -domtree -sroa -basicaa -aa -memoryssa -early-cse-memssa -domtree -basicaa -aa -lazy-value-info -jump-threading -correlated-propagation -simplifycfg -domtree -basicaa -aa -loops -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -libcalls-shrinkwrap -loops -branch-prob -block-freq -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -pgo-memop-opt -domtree -basicaa -aa -loops -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -tailcallelim -simplifycfg -reassociate -domtree -loops -loop-simplify -lcssa-verification -lcssa -basicaa -aa -scalar-evolution -loop-rotate -licm -loop-unswitch -simplifycfg -domtree -basicaa -aa -loops -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -loop-simplify -lcssa-verification -lcssa -scalar-evolution -indvars -loop-idiom -loop-deletion -loop-unroll -mldst-motion -aa -memdep -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -gvn -basicaa -aa -memdep -memcpyopt -sccp -domtree -demanded-bits -bdce -basicaa -aa -loops -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -lazy-value-info -jump-threading -correlated-propagation -domtree -basicaa -aa -memdep -dse -loops -loop-simplify -lcssa-verification -lcssa -aa -scalar-evolution -licm -postdomtree -adce -simplifycfg -domtree -basicaa -aa -loops -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -barrier -elim-avail-extern -basiccg -rpo-functionattrs -globalopt -globaldce -basiccg -globals-aa -float2int -domtree -loops -loop-simplify -lcssa-verification -lcssa -basicaa -aa -scalar-evolution -loop-rotate -loop-accesses -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -loop-distribute -branch-prob -block-freq -scalar-evolution -basicaa -aa -loop-accesses -demanded-bits -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -loop-vectorize -loop-simplify -scalar-evolution -aa -loop-accesses -loop-load-elim -basicaa -aa -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -simplifycfg -domtree -loops -scalar-evolution -basicaa -aa -demanded-bits -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -slp-vectorizer -opt-remark-emitter -instcombine -loop-simplify -lcssa-verification -lcssa -scalar-evolution -loop-unroll -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -loop-simplify -lcssa-verification -lcssa -scalar-evolution -licm -alignment-from-assumptions -strip-dead-prototypes -globaldce -constmerge -domtree -loops -branch-prob -block-freq -loop-simplify -lcssa-verification -lcssa -basicaa -aa -scalar-evolution -branch-prob -block-freq -loop-sink -lazy-branch-prob -lazy-block-freq -opt-remark-emitter -instcombine -div-rem-pairs -simplifycfg

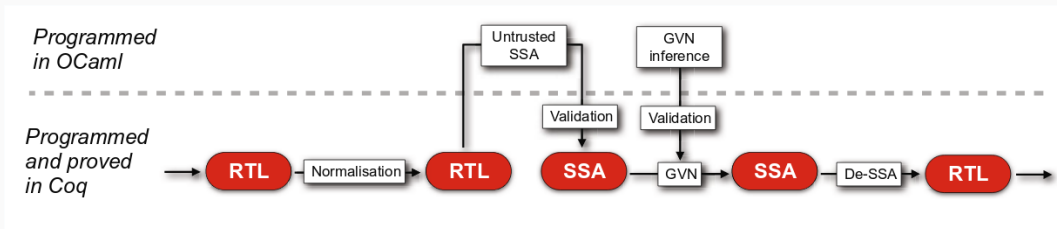
Intermediate Representations can help!

- IRs decompose compilation : simplification & modularity (proofs Compcert)
- Property : simplify analyses and transformations (SSA)
- Design and juggle with IRs (helped with validators : CompcertSSA, LLVM pipeline)
- Refine static analyses



CompcertSSA : a open door!

Opportunity for new analysis/optimizations and new IRs



Transformation SSA validated a posteriori

Focus on dependences and values

SSA

(1988)

...

$x = 1$

loop :

$\beta = \phi(x, x')$

$x' = \beta + 1$

$c = x' < 42$

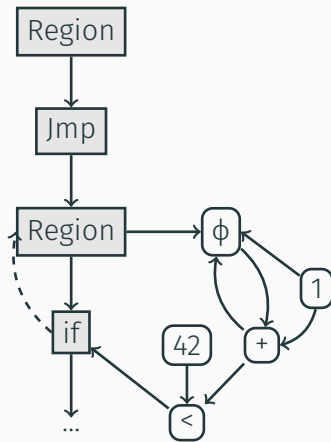
if c **loop exit**

exit :

...

Sea-of-Nodes

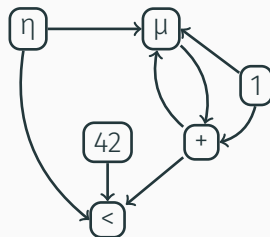
(Cliff Click 1995)



(HotSpot- Graal, LibFirm)

Synchronous Value Graph (Gated SSA)

(Paul Govereau 2011)



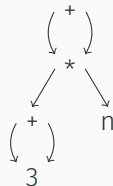
that's what I present now...

Value Graphs for validation ?

Maximal sharing on graphs

Simple example :

```
x_1 = 3 + 3  
x_2 = a * x_1  
x_3 = x_2 + x_2
```



Optimized simple example :

```
y_1 = a * 6  
y_2 = y_1 << 1
```



General $(3 + 3)$ and compiler-related $(x + x)$ reductions make the graphs converging

Maximal sharing on graphs

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Maximal sharing on graphs

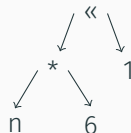
Simple example :

```
x_1 = 3 + 3  
x_2 = a * x_1  
x_3 = x_2 + x_2
```



Optimized simple example :

```
y_1 = a * 6  
y_2 = y_1 << 1
```



General $(3 + 3)$ and compiler-related $(x + x)$ reductions make the graphs converging

Each variable is assigned **exactly once**, every variable is defined before it is used :
referential transparency

Source program

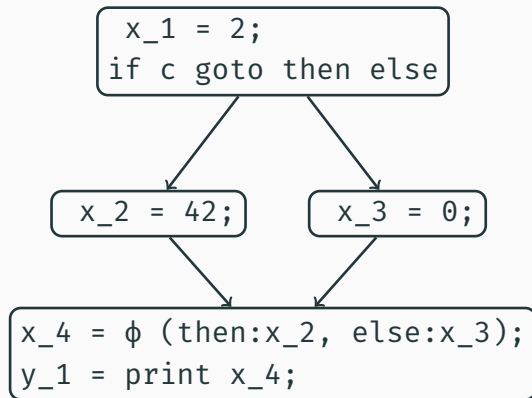
```
x = 0
y = x + 1
x = 1
z = x + 1
```

SSA program

```
x_1 = 0
y = x_1 + 1
x_2 = 1
z = x_2 + 1
```

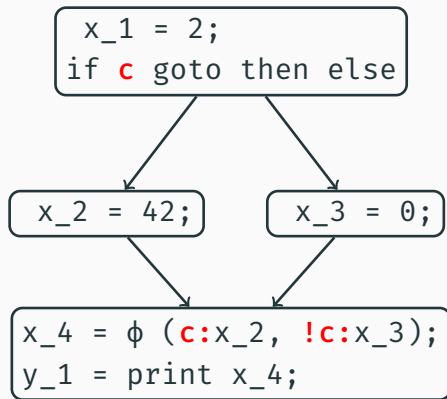
Context (2) SSA = ϕ

- ϕ -function choose the right value depending on the control flow
- Make the dependences explicit



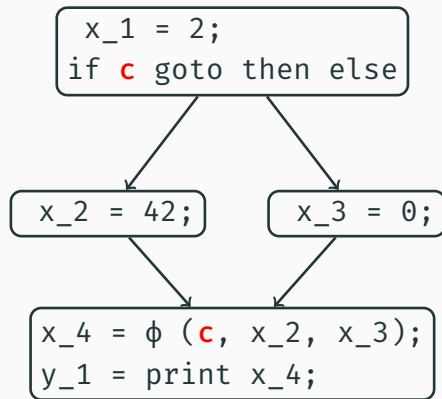
GSA : Gated Single Assignment [Ballance & al. SIGPLAN'90]

- Include **control information in ϕ**
- Simplify symbolic analyses



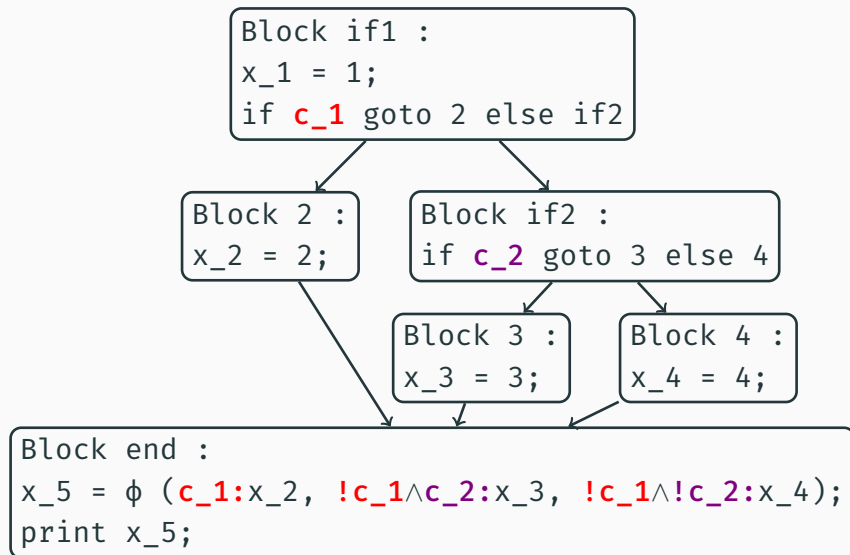
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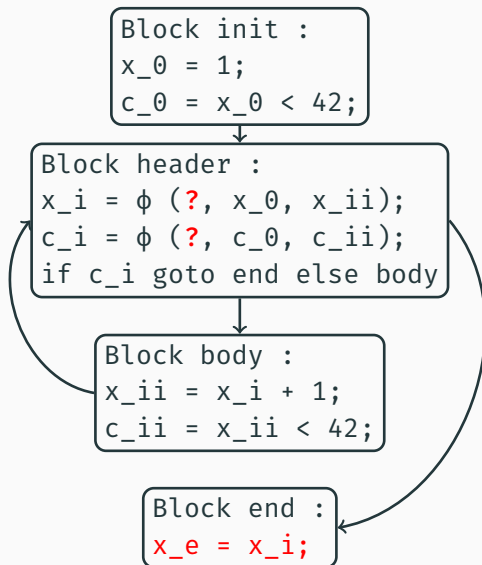
Gating ϕ

Gathering conditions for each predecessor until reaching immediate dominator



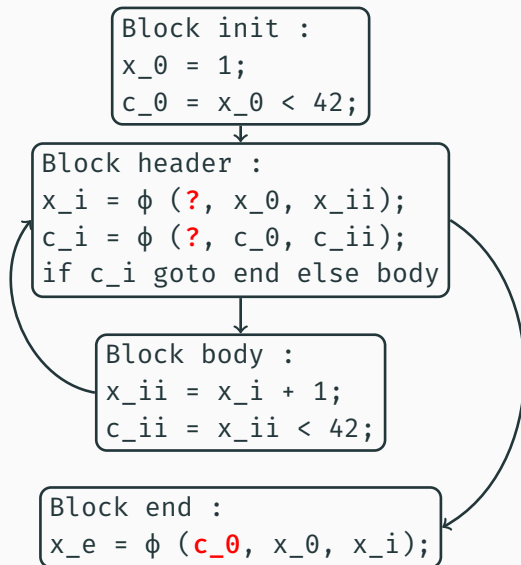
Gating Loops (μ & η)

A symbolic value for x_e ? What guard for ϕ ?



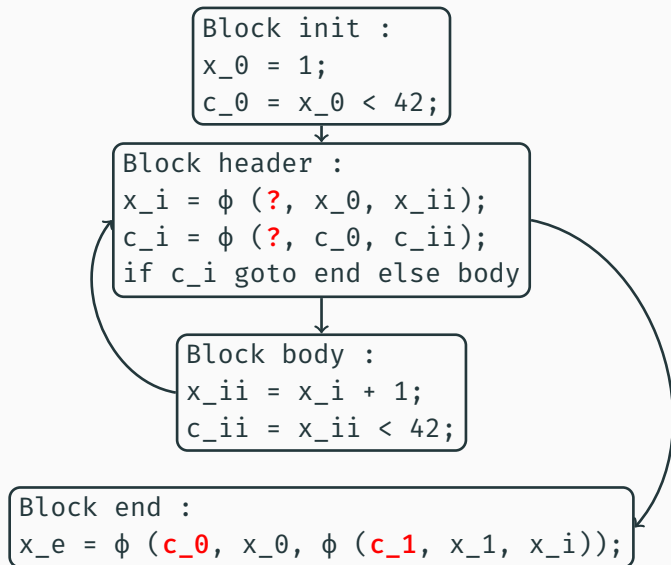
Gating Loops (μ & η)

If no iteration it should be ...



Gating Loops (μ & η)

First iteration should be ...



Gating Loops (μ & η)

N^{th} iteration should be ...

```
Block init :  
x_0 = 1;  
c_0 = x_0 < 42;
```

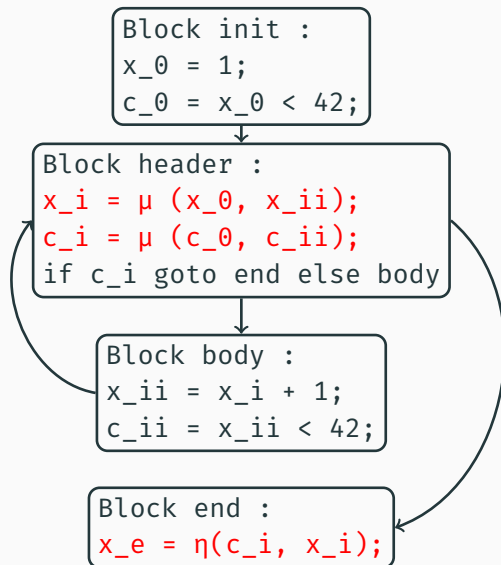
```
Block header :  
x_i =  $\phi$ (?, x_0, x_ii);  
c_i =  $\phi$ (?, c_0, c_ii);  
if c_i goto end else body
```

```
Block body :  
x_ii = x_i + 1;  
c_ii = x_ii < 42;
```

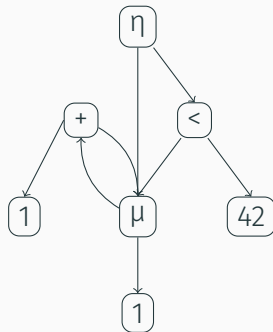
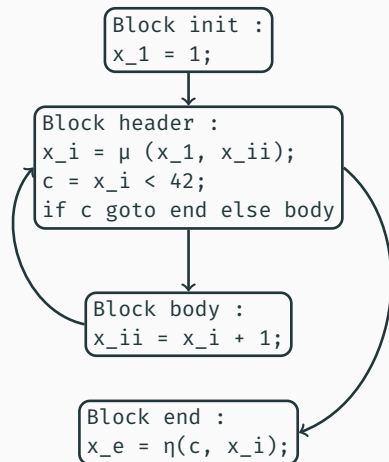
```
Block end :  
x_e =  $\phi$ (c_0, x_0,  $\phi$ (c_1, x_1, ... $\phi$ (c_n, x_n, x_i)...));
```

Gating Loops (μ & η)

μ initializes and defines variables modified in loops. η sets the out value with the guard.

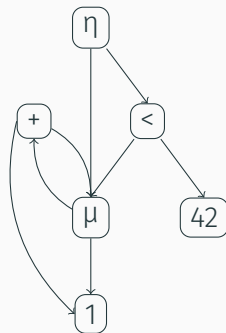
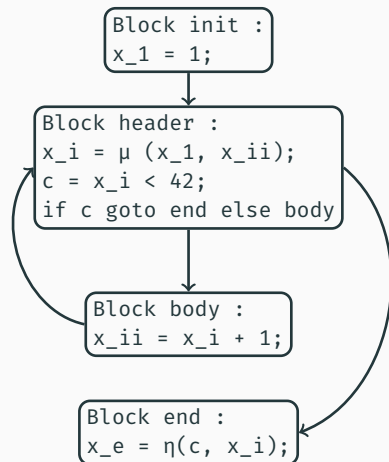


Synchronous Value Graph : building and hash-consing



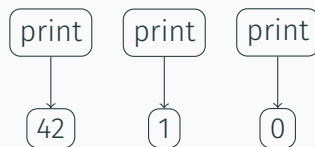
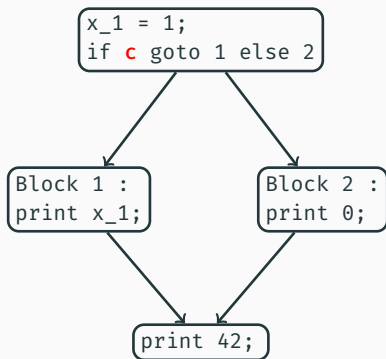
GVN for free!

Synchronous Value Graph : building and hash-consing



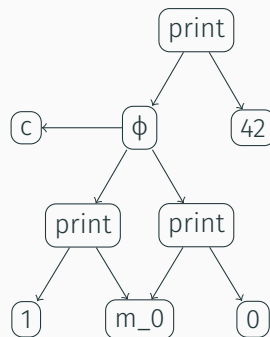
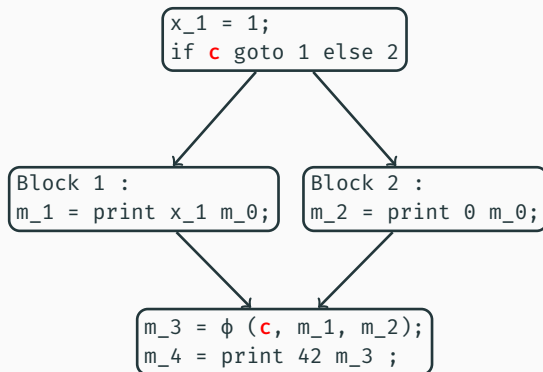
GVN for free!

How do we control side effects?



State dependency : MSSA

Introduction of abstract state variable m catching control dependencies between effects.



General rules

- $a = a \downarrow \text{true}$
- $a \neq a \downarrow \text{false}$
- ...

Optimization specific rules

- $a + a \downarrow a \ll 1$
- $a * 4 \downarrow a \ll 2$
- $\phi(\dots, \text{true}: x, \dots) \downarrow x$
- $\phi(\dots, \text{false}: x, \dots) \downarrow \phi(\dots, \dots)$
- $\phi(\dots:x, \dots:x, \dots:x, \dots) \downarrow x$
- $\eta(\text{false}, x, y) \downarrow x$
- $\eta(c, \mu(x, x)) \downarrow x$
- $\eta(c, y=\mu(x, y)) \downarrow x$

General rules

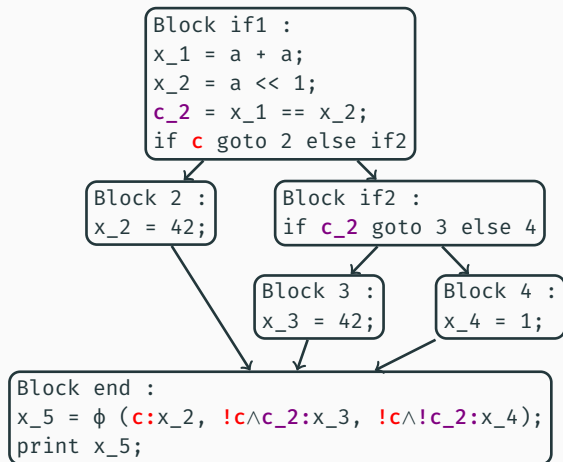
- $a = a \downarrow \text{true}$
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Optimization specific rules

- $a + a \downarrow a \ll 1$
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- $\phi(\dots, \text{true}: x, \dots) \downarrow x$
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- $\phi(\dots:x, \dots:x, \dots:x, \dots) \downarrow x$
- $\eta(\text{false}, x, y) \downarrow x$
- $\eta(c, \mu(x, x)) \downarrow x$
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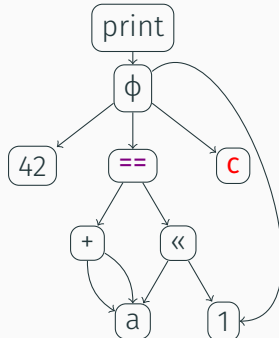
Mirror compiler optimization pipeline
(transformations order matter)!

Reduction/rewrite rules : quick example



Simplify

$\phi(c:x_2, !c^c_2:x_3, !c^!c_2:x_4)$



Reduction/rewrite rules : quick example

```
Block if1 :  
x_1 = a + a;  
x_2 = a << 1;  
c_2 = x_1 == x_2;  
if c goto 2 else if2
```

```
Block 2 :  
x_2 = 42;
```

```
Block if2 :  
if c_2 goto 3 else 4
```

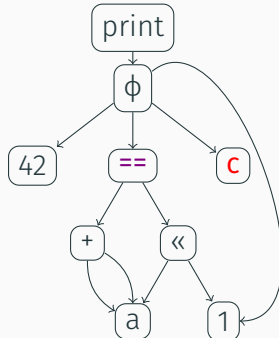
```
Block 3 :  
x_3 = 42;
```

```
Block 4 :  
x_4 = 1;
```

```
Block end :  
x_5 =  $\phi$ (c:x_2, !c^&c_2:x_3, !c^&!c_2:x_4);  
print x_5;
```

Next rule : $a + a \downarrow a \ll 1$

$\phi(c:42, !c \wedge (a+a) == (a \ll 1):42, !c \wedge !(a+a) == (a \ll 1):1)$



Reduction/rewrite rules : quick example

```
Block if1 :  
x_1 = a << 1;  
x_2 = a << 1;  
c_2 = x_1 == x_2;  
if c goto 2 else if2
```

```
Block 2 :  
x_2 = 42;
```

```
Block if2 :  
if c_2 goto 3 else 4
```

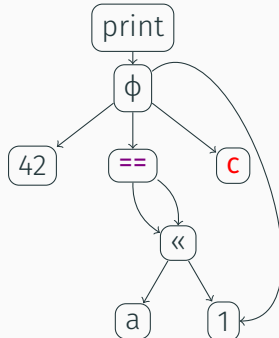
```
Block 3 :  
x_3 = 42;
```

```
Block 4 :  
x_4 = 1;
```

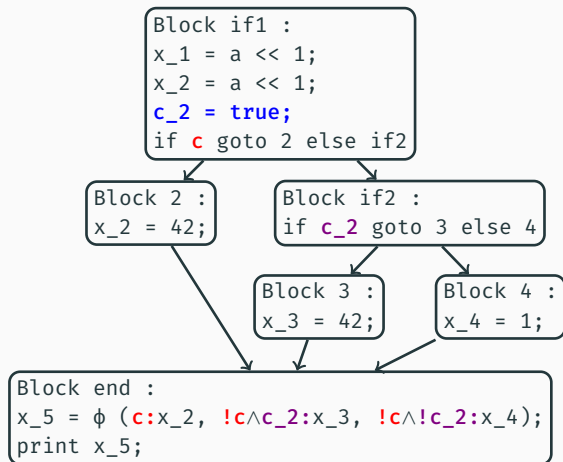
```
Block end :  
x_5 =  $\phi$ (c:x_2, !c^&c_2:x_3, !c^&!c_2:x_4);  
print x_5;
```

Next rule : $a = a \downarrow \text{true}$

$\phi(c:42, !c \wedge (a << 1) == (a << 1):42, !c \wedge !(a << 1) == (a << 1):1)$

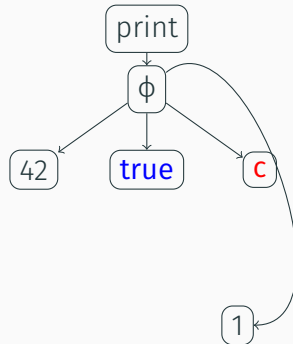


Reduction/rewrite rules : quick example

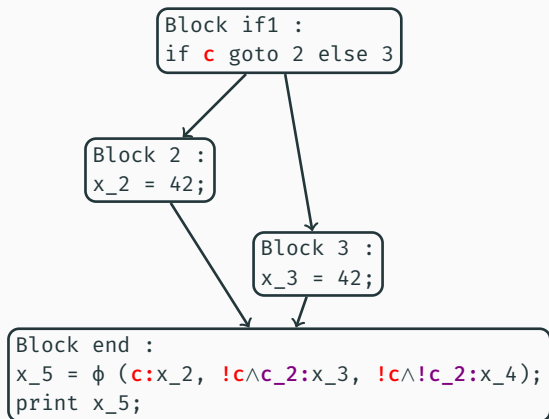


Next rule: $\phi(\dots, \text{false}: x, \dots)$

$\phi(c:42, !c \wedge (\text{true}):42, !c \wedge !(\text{true}):1)$

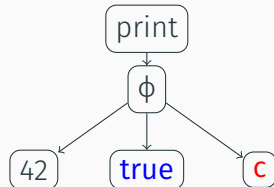


Reduction/rewrite rules : quick example



Next rule : $\phi(\dots:x, \dots:x, \dots:x, \dots) \downarrow x$

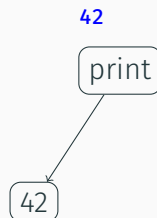
$\phi(\mathbf{c}:42, \mathbf{!c}\wedge(\mathbf{true}):42)$



Reduction/rewrite rules : quick example

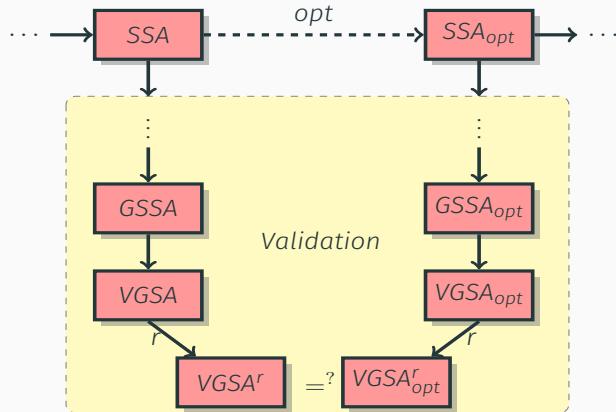
```
Block end :  
print 42;
```

Nothing to do ...



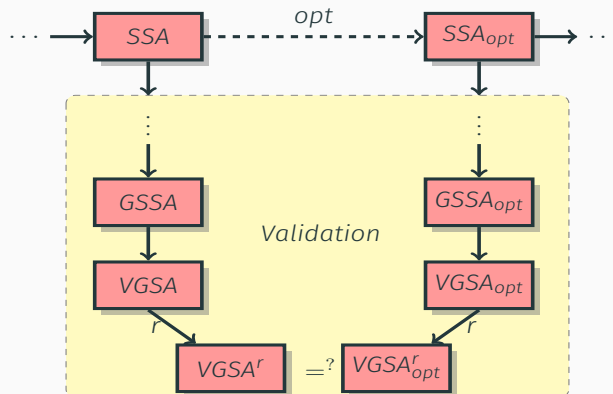
In CompcertSSA

- Has been implemented on CompcertSSA (Ocaml)
- Compromises done on loops detection...
- Validate GVN and SCCP on our tests (when loop analysis is ok)



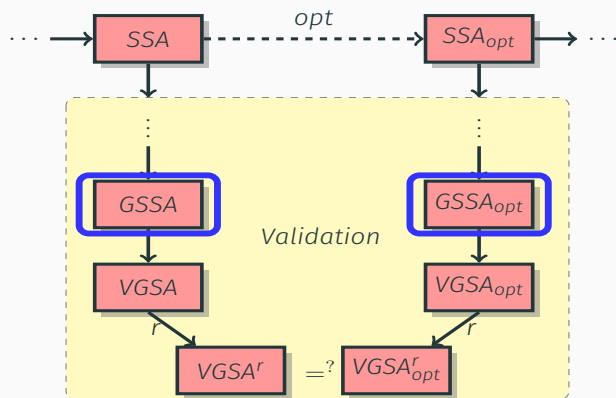
Conclusion

Formal part is still under construction...

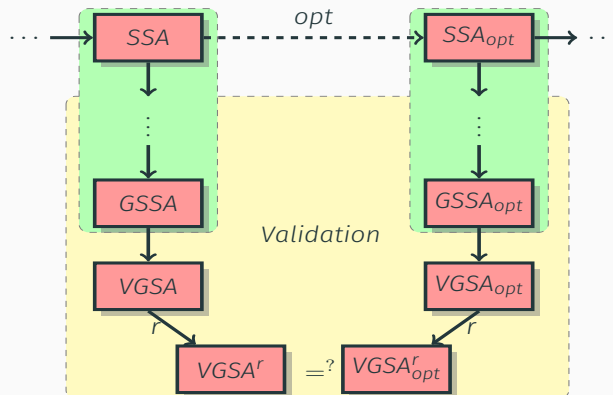


To be continued!

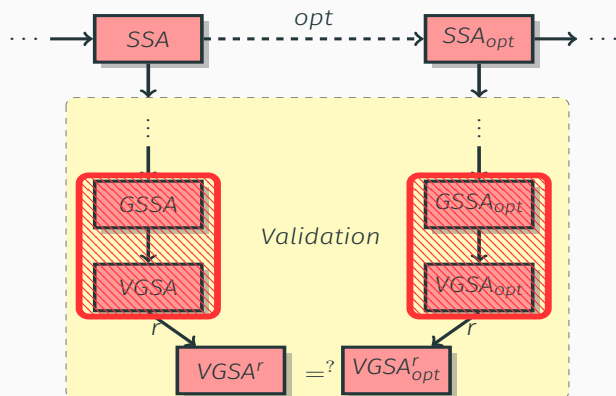
GSSA semantic OK!



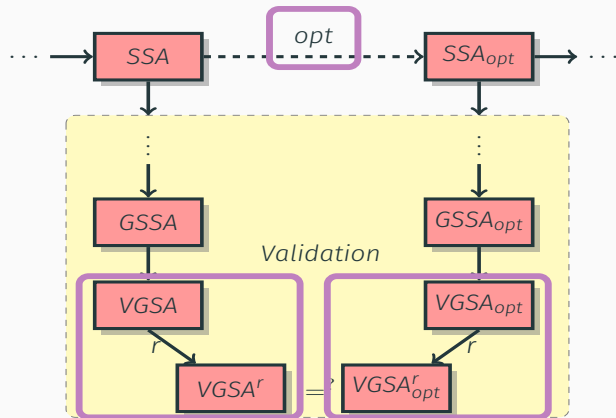
Connecting to the SSA semantic should be ok...



VGSA semantic not correct...



Validate more rules regarding to new optimizations



Questions?

Sémantique GSSA

$$\text{condT} : \frac{P(b)[pc] = (\text{lcond cond args ifso ifnot}) \quad \text{evalcond cond args} - \text{Vr} = \text{True}}{P \vdash (b, pc, \text{Vr}, m) \Rightarrow (\text{ifso}, 0, \text{Vr}, m)}$$

$$\text{condF} : \frac{P(b)[pc] = (\text{lcond cond args ifso ifnot}) \quad \text{Vr}(\text{args}) = \text{vargs evalcond cond vars} = \text{False}}{P \vdash (b, pc, \text{Vr}, m) \Rightarrow (\text{ifnot}, 0, \text{Vr}, m)}$$

$$\text{phis} : \frac{P(b)[pc] = (\text{lphis memphi phis}) \quad \text{memphi} = (((cs_1, m_1), \dots, (cs_n, m_n)), m') \quad \text{phi}_{k_r} \in \text{phis}, \text{phi}_{k_r} = (((cs_{k_1}, r_{k_1}), \dots, (cs_{k_n}, r_{k_n})), \text{res}_k) \quad t \in [1 \dots n] \quad m = m_t \quad \text{Vr}(r_{k_t}) = v_{k_t}}{P \vdash (b, pc, \text{Vr}, m) \Rightarrow (b, pc + 1, \forall(k, t) \text{Vr}[\text{res}_k \leftarrow v_{k_t}], m)}$$

$$\text{mus} : \frac{P(b)[pc] = (\text{Imu memu mus}) \quad \text{memu} = (m_0, m_i, m') \quad \text{mu}_k \in \text{mus}, \text{mu}_k = (r_{k_0}, r_{k_i}, \text{res}_k) \quad m = m_0 \Rightarrow \text{Vr}(r_{k_0}) = v_k \quad m = m_i \Rightarrow \text{Vr}(r_{k_i}) = v_k}{P \vdash (b, pc, \text{Vr}, m) \Rightarrow (b, pc + 1, \forall k \text{Vr}[\text{res}_k \leftarrow v_k], m')}$$

$$\text{etas} : \frac{P(b)[pc] = (\text{leta etas}) \quad \text{eta}_k \in \text{etas}, \text{eta}_k = (c_k, r_k, \text{res}_k) \quad \text{evalcond } c_k = \text{True}, \text{Vr}(r_k) = v_k}{P \vdash (b, pc, \text{Vr}, m) \Rightarrow (b, pc + 1, \forall k \text{Vr}[\text{res}_k \leftarrow v_k], m)}$$

$$\text{obs} : \frac{P(b)[pc] = (\text{lobs } r \text{ res } m \text{ m}') \quad \text{Vr}(r) = \text{vr} \quad \text{call vr } m \text{ vres } e}{P \vdash (b, pc, \text{Vr}, m) \stackrel{e}{\Rightarrow} (b, pc + 1, \text{Vr}[\text{res} \leftarrow \text{vres}], m')}$$

$$\text{return} : \frac{P(b)[pc] = (\text{lreturn } r \text{ m } m')}{P \vdash (b, pc, \text{Vr}, m) \Rightarrow (\text{Vr}(r), m')}$$

$$\begin{array}{c} \text{evt-step} \frac{\text{eval}_n(i)(n) = ((_, \text{true}), e)}{G, P \vdash (i, \text{eval}_n(i)) \xrightarrow{e} (i+1, \text{eval}_n(i+1))} \\ \text{\epsilon-step} \frac{\text{eval}_n(i)(n) = (_, \epsilon)}{G, P \vdash (i, \text{eval}_n(i)) \Rightarrow (i+1, \text{eval}_n(i+1))} \end{array}$$

Le langage

```
type instructions =  
| Icst of int * reg  
| Iop of op * reg * reg * reg  
| Icond of cond * reg list * label * label  
| Iphis of ((cond list * memreg) list * memreg) * ((cond list * reg) list * reg) list  
| Imus of (memreg * memreg * memreg) * (reg * reg * reg) list  
| Ieta of cond * reg * reg  
| Iobs of reg * reg * memreg * memreg  
| Ijmp of label  
| Ireturn of reg option * memreg * memreg
```