

Loop Quasi-Invariant Chunk Motion

by peeling with statement composition

Thomas Rubiano

From an idea of L. Kristiansen

supervised by J. Y. Moyen

in collaboration with T. Seiller

funded by the Elica project



ICC implementation in Compilers

ICC techniques in a loop optimization

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Welcome to the real world !



- This work shows that we can do something in real world languages
- Using data flow analysis seen in ICC papers (“size-change graphs” and “*mwp*-bounds”)



Motivations



Loop-Invariant

```
int x=rand()%100;
while(i<100){
    y=x+x; //invariant
    use(y);
    i=i+1;
}
```



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    i=i+1;
}
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    i=i+1;
}
```

- Obviously already in compilers : called “*Loop Invariant Code Motion*”
(**32111** instructions hoisted over **3808** loops in *vim*...)



Loop-Quasi-Invariants

```
while (i<100) {  
    z=y*y; //quasi-invariant  
    use (z) ;  
    y=x+x; //invariant  
    use (y) ;  
    i=i+1;  
}
```



Loop-Quasi-Invariants

```
while (i<100) {  
    z=y*y; //quasi-invariant  
    use (z);  
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    use (y);  
    i=i+1;  
}
```

```
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    z=y*y;  
    use (z);  
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    use (z);  
    use (y);  
    i=i+1;  
}
```



Loop-Quasi-Invariants

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while (i<100) {  
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```
if (i<100) {  
    z=y*y;  
    use (z) ;  
    y=x+x;  
    use (y) ;  
    i=i+1;  
}  
if (i<100) {  
    z=y*y;  
    use (z) ;  
    use (y) ;  
    i=i+1;  
}  
while (i<100) {  
    use (z) ;  
    use (y) ;  
    i=i+1;  
}
```

- Peeling is removing instructions out of the loop while unrolling it
- Done but not done...

... regarding to invariants (only loop size and trip count)!



Loop-Quasi-Invariant Chunks

```
while (j<100) {  
    fact=1;  
    i=1;  
    while (i<=n) {  
        fact=fact*i;  
        i=i+1;  
    }  
    use (fact) ;  
    j=j+1;  
}
```



Loop-Quasi-Invariant Chunks

```
while (j<100) {  
    fact=1;  
    i=1;  
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        fact=fact*i;  
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```
while (j<100) {  
    use (fact) ;  
    j=j+1;  
}
```



Loop-Quasi-Invariant Chunks

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if (j<100) {  
    fact=1;  
    i=1;  
    while (i<=n) {  
        fact=fact*i;  
        i=i+1;  
    }  
    use (fact) ;  
    j=j+1;  
}  
while (j<100) {  
    use (fact) ;  
    j=j+1;  
}
```



Loop-Quasi-Invariant Chunks

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while (j<100) {  
    fact=1;  
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if (j<100) {  
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        fact=fact*i;  
        i=i+1;  
    }  
    use (fact) ;  
    j=j+1;  
}  
while (j<100) {  
    use (fact) ;  
    j=j+1;  
}
```

- Definitely new !



Introduction



A WHILE-language

(Variables) X ::= $X_1 \mid X_2 \mid X_3 \mid \dots \mid X_n$
(Expression) exp ::= $X \mid op(exp, \dots, exp)$
(Command) com ::= $X=exp \mid com;com \mid skip \mid$
 $while\ exp\ do\ com \mid$
 $if\ exp\ then\ com\ else\ com \mid$



A WHILE-language

(Variables)	X	$::=$	$X_1 \mid X_2 \mid X_3 \mid \dots \mid X_n$
(Expression)	exp	$::=$	$X \mid op(exp, \dots, exp)$
(Command)	com	$::=$	$X=exp \mid com;com \mid skip \mid$ $while\ exp\ do\ com \mid$ $if\ exp\ then\ com\ else\ com \mid$ $use(X_1, \dots, X_n)$



Quasi-Invariants

- A quasi-invariant is a variable with a value which does not change after a certain number of loop execution
- A degree of invariance is the number of time we need to iterate the loop until the variable is stable

```
while (i<100) {  
    z=y*y; // 2  
    use (z);  
    y=x+x; // 1  
    use (y);  
    i=i+1;  
}
```



Theory : Data Flow Graph



Definition

Definition (Data Flow Graph)

A Data Flow Graph represents dependencies between variables as a bipartite graph as below.

`c := [x = x + 1;`

`y = y;`

`z = 0;]`

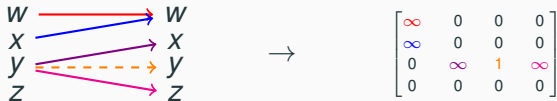
$X \xrightarrow[\infty]{\text{dependence}} X$

$y \xrightarrow[1]{\text{propagation}} y$

$Z \xrightarrow[0]{\text{reinitialization}} Z$



A *Data Flow Graph* for a command C is a $n \times n$ matrix over the semi-ring $\{0, 1, \infty\}$.

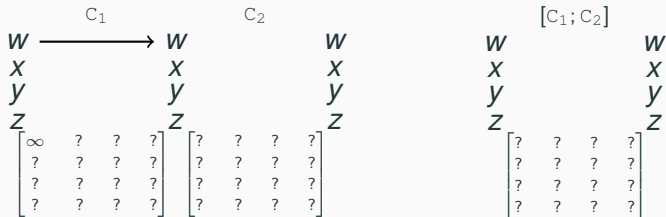


We write $+$ and \times the two operations (*max*, \times).



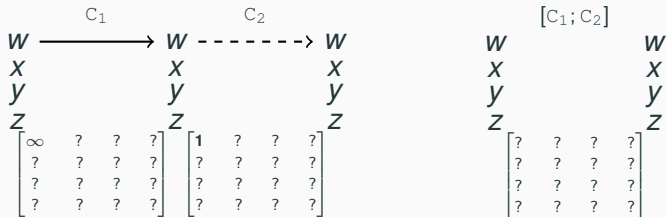
Multipath and Composition (à la “size-change Termination”)

Let C be a sequence of commands $[C_1; C_2; \dots; C_n]$. Then $M(C)$ is defined as the matrix product $M(C_1)M(C_2) \dots M(C_n)$.



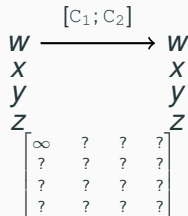
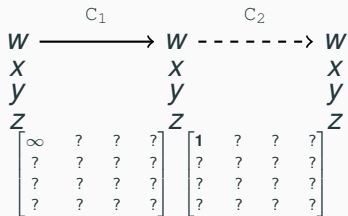
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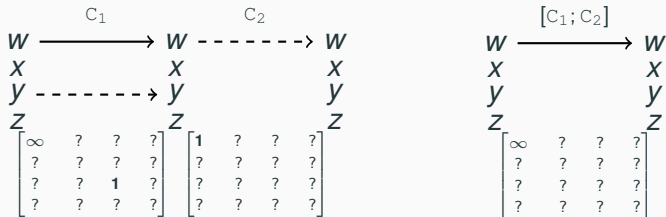
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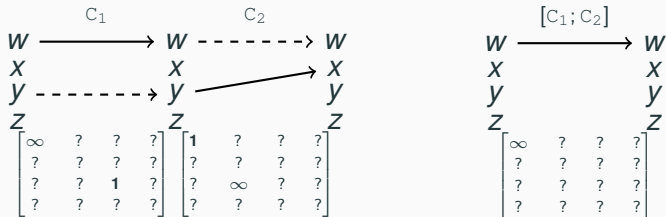
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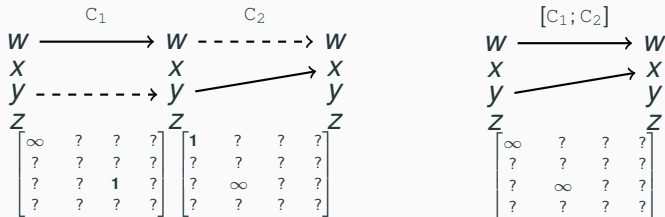
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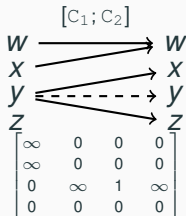
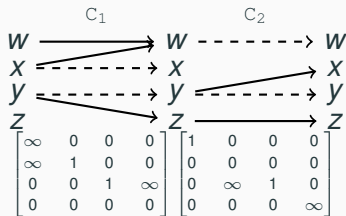
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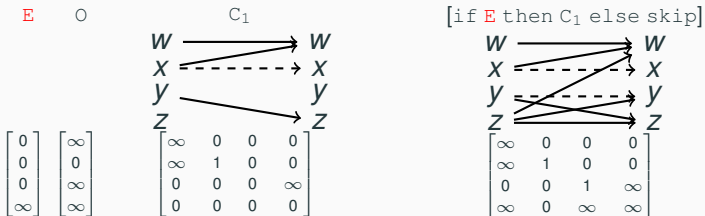
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Let C be a sequence of commands $[C_1; C_2; \dots; C_n]$. Then $M(C)$ is defined as the matrix product $M(C_1)M(C_2) \dots M(C_n)$.



Condition

Let C be a command of the form `if E then C_1 else skip`;
Then $M(C) = M(C_1) + Id + (E^t O)$



Compute the max DFG regarding to the different possibilities.
 $\text{Var}(E)$ indirectly influence the dependencies.



Loop while (à la “mwp-polynomials”)

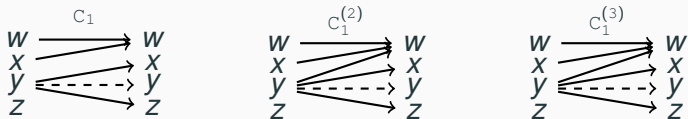
Let C be a command such as $C := \text{while } E \text{ do } C_1;$

- Number of iteration unknown :

skip C_1 $C_1; C_1$ $C_1; C_1; C_1$ etc...

- Compute the max :

$M(C_1^*)$



Trivially converges by monotonicity



Loop `while` (à la “*mwp-polynomials*”)

Let C be a command such as : $C := \text{while } E \text{ do } C_1;$

As for the `if` statement, a condition correction is needed.

$$M(C) = M(C_1^*)^{[E]}.$$



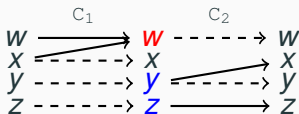
Theory : Independence



Independence of chunks

Definition (independence)

If $\text{Out}(C_1) \cap \text{In}(C_2) = \emptyset$ then C_2 is **independent** from C_1 . This is denoted $C_1 \prec C_2$.



Definition (self-independence)

If C_1 is independent from itself, we say C_1 is **self-independent**

Lemma (Optimization for while)

If C_1 is self-independent and $\text{Var}(E) \cap \text{Out}(C_1) = \emptyset$:

$\llbracket \text{while } E \text{ do } [C_1] \rrbracket \equiv \llbracket \text{if } E \text{ then } [C_1]; \text{While } E \text{ do } [\text{skip}] \rrbracket$



Moving Independent Chunks

Definition (Mutual Independence)

If $C_2 \prec C_1$ and $C_1 \prec C_2$, we say that C_2 and C_1 are **mutually independent**, and write $C_1 \succcurlyeq C_2$.

Lemma (Swapping commands)

If $C_1 \succcurlyeq C_2$, then :

$$\llbracket C_1; C_2 \rrbracket \equiv \llbracket C_2; C_1 \rrbracket$$

Lemma (Hoisting mutual independent commands)

If C_1 is self-independent (i.e. $C_1 \succcurlyeq C_1$), $\text{Var}(E) \cap \text{Out}(C_1) = \emptyset$, and if $C_1 \succcurlyeq C_2$, then :

$$\llbracket \text{while } E \text{ do } [C_1; C_2] \rrbracket \equiv \llbracket \text{if } E \text{ then } [C_1]; \text{while } E \text{ do } [C_2] \rrbracket$$



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$$\llbracket \text{while } E \text{ do } [C_1; C_2] \rrbracket \equiv \llbracket \text{if } E \text{ then } [C_1; C_2]; \text{while } E \text{ do } [C_2] \rrbracket$$



Computation of the invariance degree

Statically easy using the DFGs and the dominance graph (order of the instructions).

Let suppose we have computed the graph of dependencies for all commands.

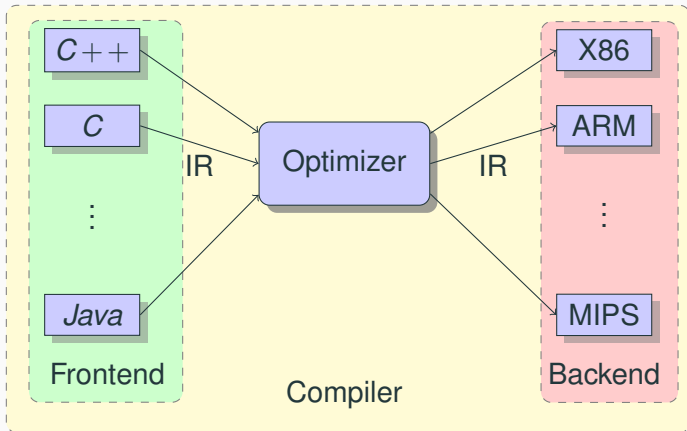
Compute recursively (depth-first order) the degrees of the depended commands and take the maximum.



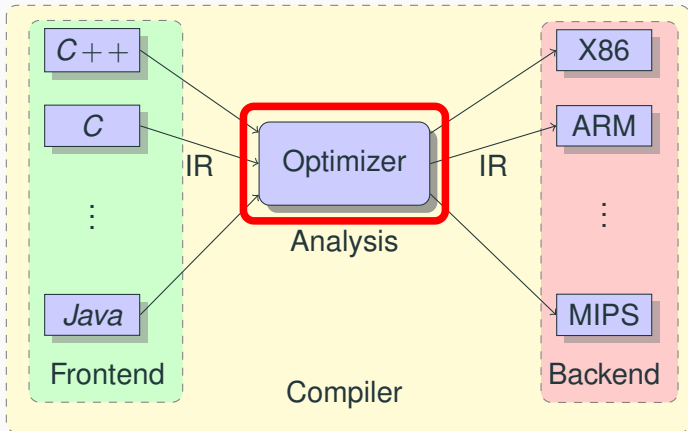
Compiler



Architecture



Architecture



Order is given as argument to the **pass manager** :

```
$ clang -O3 test.c
```



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```
$ clang -O3 test.c
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```
Pass Arguments: -targetlibinfo -no-aa -tbaa -scoped-noalias -assumption-tracker  
-basicaa -notti -verify-di -ipsccp -globalopt -deadargelim -domtree  
-instcombine -simplifycfg -basiccg -prune-eh -inline-cost -inline  
-functionattrs -argpromotion -sroa -domtree -early-cse -lazy-value-info  
-jump-threading -correlated-propagation -simplifycfg -domtree -instcombine  
-tailcallelim -simplifycfg -reassociate -domtree -loops -loop-simplify -lcssa  
-loop-rotate -licm -loop-unswitch -instcombine -scalar-evolution  
-loop-simplify -lcssa -indvars -loop-idiom -loop-deletion -function_tti  
-loop-unroll -memdep -mldst-motion -domtree -memdep -gvn -memdep -memcpyopt  
-sccp -domtree -instcombine -lazy-value-info -jump-threading  
-correlated-propagation -domtree -memdep -dse -adce -simplifycfg -domtree  
-instcombine -barrier -domtree -loops -loop-simplify -lcssa -branch-prob  
-block-freq -scalar-evolution -loop-vectorize -instcombine -scalar-evolution  
-slp-vectorizer -simplifycfg -domtree -instcombine -loops -loop-simplify  
-lcssa -scalar-evolution -function_tti -loop-unroll  
-alignment-from-assumptions -strip-dead-prototypes -globaldce -constmerge  
-verify -verify-di
```



Order is given as argument to the **pass manager** :

```
$ clang -O3 test.c
```

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```



LLVM Intermediate Representation

- LLVM-IR is a **Typed Assembly Language** (TAL) and a **Static Single Assignment** (SSA) based representation. This provides :
- An IR is **source-language-independent**, then optimizations and analysis should work on every languages (properly translated to this IR).



LLVM Intermediate Representation

```
define i32 @main() #0 {
entry:
  %call = call i64 @time(i64* null) #3
  %conv = trunc i64 %call to i32
  call void @srand(i32 %conv) #3
  %call1 = call i32 @rand() #3
  %rem = srem i32 %call1, 100
  %call2 = call i32 @rand() #3
  br label %while.cond

while.cond:
  %i.0 = phi i32 [ 0, %entry ], [ %inc, %while.body ]
  %y.0 = phi i32 [ 0, %entry ], [ %add, %while.body ]
  %exitcond = icmp ne i32 %i.0, 100
  br i1 %exitcond, label %while.body, label %while.end

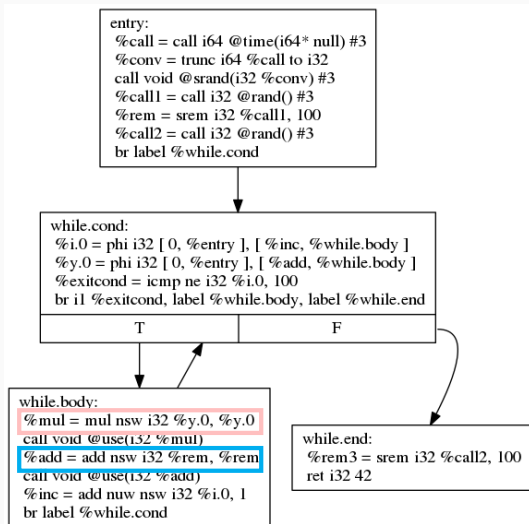
while.body:
  %mul = mul nsw i32 %y.0, %y.0
  call void @use(i32 %mul)
  %add = add nsw i32 %rem, %rem
  call void @use(i32 %add)
  %inc = add nuw nsw i32 %i.0, 1
  br label %while.cond

while.end:
  %rem3 = srem i32 %call2, 100
  ret i32 42
}
```

```
int main(){
  int i=0,y=0;
  srand(time(NULL));
  int x=rand()%100;
  int x2=rand()%100;
  int z;
  while(i<100){
    z=y*y;
    use(z);
    y=x+x;
    use(y);
    i++;
  }
  return 42;
}
```



LLVM Intermediate Representation in Control Flow Graph



CFG for 'main' function

```
int main() {  
    int i=0,y=0;  
    srand(time(NULL));  
    int x=rand()%100;  
    int x2=rand()%100;  
    int z;  
    while(i<100) {  
        z=y*y;  
        use(z);  
        y=x+x;  
        use(y);  
        i++;  
    }  
    return 42;  
}
```



Implementation



A prototype on LLVM tool chain

We implemented a pass in LLVM :

- Currently around 3000 lines of C++, and counting. . .
- tested on several relevant examples
- generates statistics while compiling. . .



Analysis : Degree on each Instruction

```
...  
while.body:  
    %mul = mul nsw i32 %y.0, %y.0 ← 2  
    call void @use(i32 %mul) ← ∞  
    %add = add nsw i32 %rem, %rem ← 1  
    call void @use(i32 %add) ← ∞  
    %inc = add nuw nsw i32 %i.0, 1 ← ∞  
    br label %while.cond ← ∞  
...
```

```
...  
while(i<100){  
    z=y*y ;  
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    i++;  
}  
...
```



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...
```

```
...
while(i<100){
  z=y*y ;
  use(z);
  y=x+x ;
  use(y);
  i++;
}
...
```

Consider all `call` as anchors



Same example

```
int main(){
    int i=0,y=0;
    srand(time(NULL));
    int x=rand()%100;
    int x2=rand()%100;
    int z;
    while(i<100){
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        use(z);
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    }
    return 42;
}
```



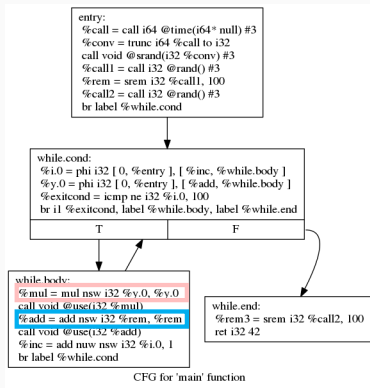
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    int z;
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        z=y*y;
        use(z);
        y=x+x;
        use(y);
        i=i+1;
    }
    if(i<100){
        z=y*y;
        use(z);
        use(y);
        i=i+1;
    }
    while(i<100){
        use(z);
        use(y);
        i=i+1;
    }
    return 42;
}
```



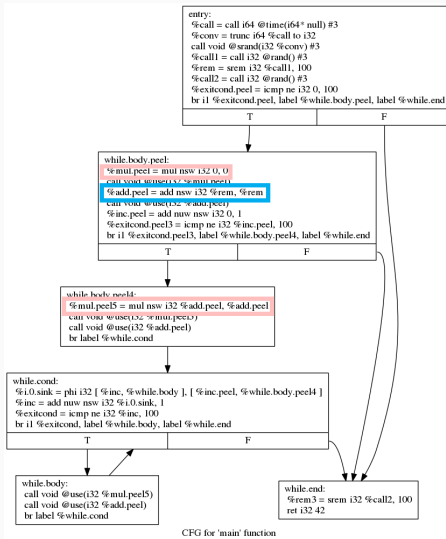
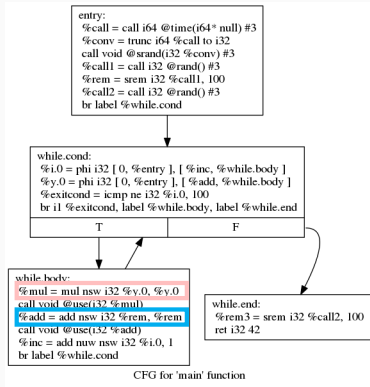
Same example



```
int main(){
    int i=0,y=0;
    srand(time(NULL));
    int x=rand()%100;
    int x2=rand()%100;
    int z;
    if (i<100){
        z=y*y;
        use(z);
        y=x+x;
        use(y);
        i=i+1;
    }
    if (i<100){
        z=y*y;
        use(z);
        use(y);
        i=i+1;
    }
    while (i<100){
        use(z);
        use(y);
        i=i+1;
    }
    return 42;
}
```



Same example



Last “relevant” example

```
while(j<100){  
    fact=1;  
    I=1;  
    while(I<=n){  
        fact=fact*I;  
        I=I+1;  
    }  
    use(fact);  
    j=j+1;  
}
```



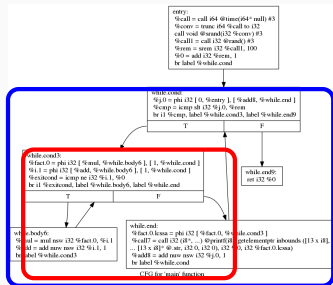
Last “relevant” example

```
while(j<100){  
    fact=1;  
    I=1;  
    while(I<=n){  
        fact=fact*I;  
        I=I+1;  
    }  
    use(fact);  
    j=j+1;  
}
```

```
if(j<100){  
    fact=1;  
    I=1;  
    while(I<=n){  
        fact=fact*I;  
        I=I+1;  
    }  
    use(fact);  
    j=j+1;  
}  
while(j<100){  
    use(fact);  
    j=j+1;  
}
```



Last “relevant” example



```
if (j<100) {
```

```
    fact=1;
```

```
    I=1;
```

```
    while (I<=n) {  
        fact=fact*I;  
        I=I+1;  
    }
```

```
    use (fact);
```

```
    j=j+1;
```

```
}  
while (j<100) {
```

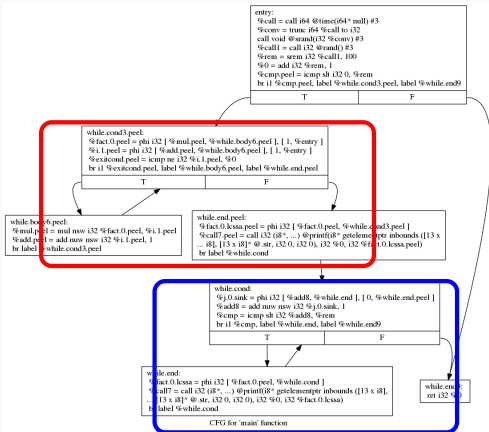
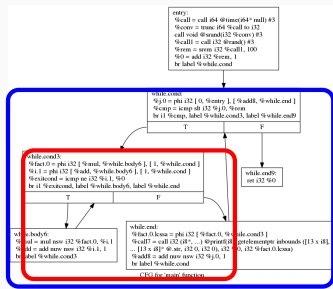
```
    use (fact);
```

```
    j=j+1;
```

```
}
```



Last “relevant” example



LLVM statistics

```
=====  
... Statistics Collected ...  
=====
```

```
2 globalopt      - Number of globals deleted  
5 globalopt      - Number of globals marked unnamed_addr  
1 indvars        - Number of congruent IVs eliminated  
2 indvars        - Number of loop exit tests replaced  
2 indvars        - Number of exit values replaced  
10 instcombine   - Number of insts combined  
1 instsimplify   - Number of redundant instructions removed  
8 lcssa          - Number of live out of a loop variables  
1 licm           - Number of instructions hoisted out of loop  
2 loop-rotate    - Number of loops rotated  
11 loop-simplify - Number of pre-header or exit blocks inserted  
2 loop-unswitch  - Total number of instructions analyzed  
1 loop-vectorize - Number of loops analyzed for vectorization  
2 lqicm          - Number of time runOnLoop is performed...  
3 lqicm          - Number of instructions with deg != -1  
1 lqicm          - Number of innerBlocks with deg != -1  
4 mem2reg        - Number of PHI nodes inserted  
2 mem2reg        - Number of alloca's promoted with a single store  
9 simplifycfg    - Number of blocks simplified
```



LLVM statistics

```
--- vim -O1 EarlyOpt 7m5,276s
3808 number of loops
20465 number of instructions hoisted by LICM
2266 number of loops with several exit blocks
125 number of loops not well formed
2391 sum of loop not analyzed
1417 sum of loop analyzed by LQICM
2476 number of quasi-invariants detected
335 number of quasi-invariants Chunk detected
23 Number of chunks with deg >= 2
```

```
--- emacs -O1 EarlyOpt 15m52,556s
3161 number of loops
16415 number of instructions hoisted by LICM
1775 number of loops with several exit blocks
150 number of loops not well formed
1925 sum of loop not analyzed
1236 sum of loop analyzed by LQICM
2197 number of quasi-invariants detected
311 number of quasi-invariants Chunk detected
35 Number of chunks with deg >= 2
```



Difficulties...

- Apprehend LLVM tools and data structure...
- Consider all strange cases we can have in LLVM-IR
- More and more features have to be implemented to be able to compete with Loop Invariant Code Motion...



Conclusion and further work

We implemented the first skeleton of a huge project

Still a lot of work to do :

- Compile a lot of programs to have more stats
- Make the pass more flexible to take into account more cases
- Start benchmarks with the transformation and compete with LICM!
- Push the compilation community to contribute ?
- mwp-polynomials is an analysis not so far. . .



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- Push the compilation community to contribute ?
- mwp-polynomials is an analysis not so far. . .
- Helping you to implement your analysis ?

